Lectures on Challenging Mathematics

RC3M2
Enhancement of Computational Mathematics
Part 2, Modulo 2

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"Cogito ergo Sum" – "I think, therefore I am"

René Descartes (1596-1650)

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Contents

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1 Algebra **1**
1.1 Challenging techniques in factoring . . . 1
1.2 More on sums and products . . . 3
1.3 Polynomials, roots, and coefficients (part 1) . . . 5
1.4 Polynomials, roots, and coefficients (part 2) . . . 7
1.5 Systems of equations (part 2) . . . 9
1.6 Algebra 4.1 . . . 11
1.7 Algebra 4.2 . . . 13
1.8 Algebra 4.3 . . . 15

2 Combinatorics **17**
2.1 Calculating in two ways and Vandermonde . . . 17
2.2 Practices with recursive counting . . . 19
2.3 Challenging counting problems from recent contests (part 1) . . . 21
2.4 Challenging counting problems from recent contests (part 2) . . . 23

3 Geometry **25**
3.1 Law of sines, area, Ceva and Menelaus (part 2) . . . 25
3.2 More on analytic geometry . . . 27
3.2.1 Vectors . . . 27
3.2.2 Parabolas . . . 27
3.3 Geometry computations (part 3) . . . 29
3.3.1 Area . . . 29
3.3.2 Mixed exercises . . . 30
3.4 Geometry computations (part 4) . . . 31
3.4.1 Similar triangles . . . 31
3.4.2 Mixed exercises . . . 32
3.5 Law of sines, area, Ceva and Menelaus (part 3) . . . 33
3.6 Challenges in solid geometry . . . 34

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4 Number Theory **37**
4.1 Reviewing modulo arithmetics via computations 37
4.1.1 Practice set 1 37
4.1.2 Practice set 2 37
4.1.3 Practice set 3 38

5 Practice Tests **39**
5.1 Selected advanced levels problems from AMC 2011 39

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