

Lectures on Challenging Mathematics

RC3M1

Enhancement of Computational Mathematics Part 2, Module 1

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“Cogito ergo Sum” – “I think, therefore I am”

René Descartes (1596-1650)

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Contents

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Algebra	1
1.1 Motion	1
1.1.1 Motion	1
1.2 Polynomial and its roots	3
1.2.1 Polynomial and its roots	3
1.2.2 Mixed exercises	4
1.3 Computations with symmetric polynomials	6
1.4 Systems of equations (part 1)	8
1.4.1 Linear systems	8
1.4.2 Systems and factoring	9
1.4.3 Additional algebra practices	9
1.5 Telescoping sums	11
1.6 Algebra 3.1	12
1.6.1 Algebra 3.1	12
1.6.2 Partial fractions (part 1)	12
1.7 Algebra 3.2	14
1.7.1 Algebra 3.2	14
1.7.2 Partial fractions (part 2)	14
1.8 Algebra 3.3	16
1.8.1 Algebra 3.3	16
1.8.2 Partial fractions (part 3)	17
2 Combinatorics	19
2.1 Challenging counting practices (part 1)	19
2.2 Challenging counting practices (part 2)	21
2.3 Challenging counting practices (part 3)	22
2.4 Challenging counting practices (part 4)	24
2.5 Challenging counting practices (part 5)	26
2.6 Challenging counting practices (part 6)	28

3	Geometry	31
3.1	Law of sines, area, Ceva and Menelaus (part 1)	31
3.1.1	Law of sines, area, Ceva and Menelaus (part 1)	31
3.1.2	Mixed computational exercises	33
3.2	Geometry computations (part 1)	34
3.2.1	A quick assessment in geometry calculations	34
3.2.2	Mixed exercises	35
3.3	Geometry computations (part 2)	36
3.3.1	Revisiting similarity	36
3.3.2	Mixed exercises	37
3.4	Lattice points and analytic geometry	38
3.5	Side lengths of cyclic quadrilaterals	40
4	Number Theory	43
4.1	Challenging AIME level Diophantine equations	43