

Lectures on Challenging Mathematics

EC2M1 Challenges in Computational Mathematics Part 2, Modulo 1

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“Cogito ergo Sum” – “I think, therefore I am”

René Descartes (1596-1650)

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