

Lectures on Challenging Mathematics

PC3 Combinatorics Essential Computational Mathematics

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“Cogito ergo Sum” – “I think, therefore I am”

René Descartes (1596-1650)

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Contents

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I	Combinatorics	3
1.1	Simple counting strategies (part 1)	3
1.1.1	Listing and Addition principle	3
1.1.2	Multiplication principle	4
1.2	Simple counting strategies (part 2)	6
1.2.1	Simple complications of addition and multiplication principles	6
1.2.2	Dealing with over counting	6
1.3	Simple counting strategies (part 3)	7
1.3.1	Permutations	7
1.3.2	Terminologies with sets (part 1)	7
1.4	Simple counting strategies (part 4)	9
1.4.1	Dealing with uniform overcounting	9
1.4.2	Terminologies with sets (part 2)	9
1.5	Simple counting strategies (part 5)	11
1.5.1	Combinations	11
1.5.2	Subtraction, overcounting, and counting complement	12
1.6	Simple counting strategies (part 6)	13
1.6.1	Number of subsets (part 1)	13
1.6.2	Does the order matter? (part 1)	13
1.7	Simple counting strategies (part 7)	14
1.7.1	Number of subsets (part 2)	14
1.7.2	Does the order matter? (part 2)	15
1.8	Simple counting strategies (part 8)	16
1.8.1	Seeing the subtle differences (part 1)	16
1.8.2	Challenging counting practice set 1	16
1.9	Simple counting strategies (part 9)	18
1.9.1	Seeing the subtle differences (part 2)	18
1.9.2	Challenging counting practice set 2	18
1.10	Simple counting strategies (part 10)	20
1.10.1	Seeing the subtle differences (part 3)	20
1.10.2	Challenging counting practice set 3	20